Kaon Interferometry: A Sensitive Probe of the QCD Equation of State?

Sven Soff[1], Steffen A. Bass[2,3], David H. Hardtke[1], and Sergey Y. Panitkin[4]
[1] *Nuclear Science Division 70-319, Lawrence Berkeley National Laboratory, 1 Cyclotron Road, Berkeley, CA94720, USA*
[2] *Department of Physics, Duke University, Durham, NC27708, USA*
[3] *RIKEN BNL Research Center, Brookhaven National Laboratory, Upton, NY11973, USA*
[4] *Physics Department, Brookhaven National Laboratory, PO Box 5000, Upton, NY11973, USA*
(September 19, 2001)

arXiv:nucl-th/0109055 v1 19 Sep 2001

We calculate the kaon HBT radius parameters for high energy heavy ion collisions, assuming a first order phase transition from a thermalized Quark-Gluon-Plasma (QGP) to a gas of hadrons. At high transverse momenta $K_T \sim 1\,\mathrm{GeV/c}$ direct emission from the phase boundary becomes important, the emission duration signal, i.e., the $R_{\mathrm{out}}/R_{\mathrm{side}}$ ratio, and its sensitivity to T_c (and thus to the latent heat of the phase transition) are enlarged. Moreover, the QGP+hadronic rescattering transport model calculations do not yield unusual large radii ($3 \leq R_i \leq 9\,\mathrm{fm}$). Finite momentum resolution effects have a strong impact on the extracted HBT parameters (R_i and λ) as well as on the ratio $R_{\mathrm{out}}/R_{\mathrm{side}}$.

In this Letter we present predictions for the kaon interferometry measurements in Au+Au collisions at the Relativistic Heavy Ion Collider (RHIC). Correlations of identical kaon pairs as well as Bose-Einstein correlations in general represent an important tool for the understanding of the space-time dynamics in multiparticle production processes [1]. In the particular case of relativistic heavy ion collisions, one important goal is to prove the existence of a phase transition from quark-gluon matter to hadrons as predicted by QCD lattice calculations for high temperatures. Moreover, the properties of that phase transition as for example the critical temperature T_c or its latent heat are of great interest. In the case of a first order phase transition, the associated large hadronization time was predicted to lead to unusually large Hanbury-Brown–Twiss (HBT) radius parameters [2–4]. The mixed phase of coexisting hadrons and partons prolongs the emission duration of particles from the phase boundary because of the large latent heat. This prolonged emission duration should then lead to an increase of the effective source size, in particular in the *outward* direction, i.e., parallel to the transverse pair velocity. This phenomenon was also expected to depend on the critical temperature T_c, the latent heat or the specific entropy of the quark-gluon phase (for recent reviews on this topic see e.g. [5,6]).

However, as demonstrated recently [7], the subsequent hadronic rescattering phase following hadronization from a thermalized QGP does not only modify the pion HBT radius parameters but even dominates them. Late numerous soft collisions in the hadronic phase diminish and also alter qualitatively the particular dependencies on the QGP-properties [7].

Here, we investigate what can be learned from the interferometry analysis of kaons. The motivation to extend the interferometry analysis from pions to kaons (which are expected to be measured soon at RHIC) is provided by several aspects: kaons are expected to be less contaminated by resonance decays compared to pions [8]. In the particular case of neutral kaon correlations, two-particle Coulomb interactions do not distort the Bose-Einstein correlations. Furthermore, the kaon density is considerably smaller than the pion density. The pion multiplicity itself has increased by approximately 70% from SPS to RHIC whereas the HBT-radii are almost the same [9,10]. Hence, higher multiparticle correlation effects that might play a role for pions, should be of minor importance for kaons. The comparison of kaon and pion correlation functions will provide a test of the presently applied two-particle correlation formalism. Another effect might arise from the strangeness distillation mechanism [11] that may further increase the time delay signature $R_{\mathrm{out}}/R_{\mathrm{side}}$. Kaon evaporation could for example lead to strong temporal emission asymmetries between kaons and antikaons [12], thus probing the latent heat of the phase transition.

We will show in the following that for kaons, similar as for the pions, the bulk properties of the two-particle correlation functions are dominated by a long-lived hadronic rescattering phase. Thus, the HBT radii appear to depend only weakly on the precise properties of the QGP, such as the thermalization time τ_i, T_c, the latent heat or the specific entropy of the QGP. However, we will demonstrate that this sensitivity is considerably enlarged at high transverse momenta $K_T \sim 1\,\mathrm{GeV/c}$. In this kinematic regime, direct emission from the phase boundary becomes important ($\sim 30\%$). The hadronic phase gets less opaque and allows us to inspect the prehadronic phase with less distortions. Finally, we will calculate explicitly the correlation functions and extract the HBT parameters with and without taking finite momentum resolution effects into account. A strong impact on the radii, the λ intercept parameter and in particular the $R_{\mathrm{out}}/R_{\mathrm{side}}$ ratio are observed; they all decrease, depending on K_T, if a finite momentum resolution is taken into account. This is important for the interpretation of experimental data and has been neglected in previous calculations addressing RHIC data.

The calculations are performed within the framework of a relativistic transport model that describes the initial dense phase of a QGP by means of ideal hydrodynamics employing a bag model equation of state that exhibits a first order phase transition [4,13]. Hence, we focus on a

phase transition in local equilibrium, proceeding through the formation of a mixed phase. Smaller radii and emission times may result for a crossover [4,14] or for a rapid out-of-equilibrium phase transition similar to spinodal decomposition [15]. Cylindrically symmetric transverse expansion and longitudinally boost-invariant scaling flow are assumed [4,13,16]. This approximation should be reasonable for central collisions at high energy, and around midrapidity. The model reproduces the measured p_T-spectra and rapidity densities of a variety of hadrons at $\sqrt{s} = 17.4A$ GeV (CERN-SPS energy), when assuming the standard thermalization (proper) time $\tau_i = 1$ fm/c, and an entropy per net baryon ratio of $s/\rho_B = 45$ [16,17]. Due to the higher density at midrapidity, thermalization may be faster at BNL-RHIC energies – here we assume $\tau_i = 0.6$ fm/c and $s/\rho_B = 200$. (With these initial conditions preliminary results on the multiplicity, the transverse energy, the p_T-distribution of charged hadrons, and the $\overline{p}/p$ ratio at $\sqrt{s} = 130A$ GeV are described quite well [16,17]; HBT correlations of pions at small relative momenta do *not* depend sensitively on these initial conditions [7].) The later hadronic phase is modeled via a microscopic transport model that allows us to calculate the so-called freeze-out, i.e., the time and coordinate space points of the last strong interactions of an individual particle species, rather than applying a freeze-out prescription as necessary in the *pure* hydrodynamic approach. Here, we employ a semi-classical transport model that treats each particular hadronic reaction channel (formation and decay of hadronic resonance states and $2 \to n$ scattering) *explicitly* [18]. The transition at hadronization is performed by matching the energy-momentum tensors and conserved currents of the hydrodynamic solution and of the microscopic transport model, respectively (for details, see [17]). The microscopic model propagates each individual hadron along a classical trajectory, and performs $2 \to n$ and $1 \to m$ processes stochastically. Meson-meson and meson-baryon cross sections are modeled via resonance excitation and also contain an elastic contribution. All resonance properties are taken from [19]. The πK cross section for example is either elastic or is dominated by the $K^*(892)$, with additional contributions from higher energy states. In this way, a good description of elastic and total kaon cross sections *in vacuum* is obtained [18]. Medium effects on the hadron properties, as for example recently studied by hydrodynamical calculations employing a chiral equation of state [14], are presently neglected. For further details of this dynamical two-phase transport model, we refer to refs. [16,17].

For the following correlation analysis, a coordinate system is used in which the *long* axis (z) is chosen parallel to the beam axis, where the *out* direction is defined to be parallel to the transverse momentum vector $\mathbf{K_T} = (\mathbf{p_{1T}} + \mathbf{p_{2T}})/2$ of the pair, and the *side* direction is perpendicular to both. Due to the definition of the *out* and *side* direction, $R_{\rm out}$ probes the spatial *and* temporal extension of the source while $R_{\rm side}$ only probes the spatial extension. Thus the ratio $R_{\rm out}/R_{\rm side}$ gives a measure of the emission duration (see also eqs.(1)-(3) and discussion below). It has been suggested that the ratio $R_{\rm out}/R_{\rm side}$ should increase strongly once the initial entropy density s_i becomes substantially larger than that of the hadronic gas at T_c [4]. The Gaussian HBT radius parameters are obtained from a saddle-point integration over the classical phase space distribution of the hadrons at freeze-out (points of their last (strong) interaction) that is identified with the Wigner density of the source, $S(x,K)$ [6,8,20].

$$R^2_{\rm side}(\mathbf{K_T}) = \langle \tilde{y}^2 \rangle(\mathbf{K_T}) \,, \tag{1}$$

$$R^2_{\rm out}(\mathbf{K_T}) = \langle (\tilde{x} - \beta_t \tilde{t})^2 \rangle(\mathbf{K_T}) = \langle \tilde{x}^2 + \beta_t^2 \tilde{t}^2 - 2\beta_t \tilde{x}\tilde{t} \rangle \,, \tag{2}$$

$$R^2_{\rm long}(\mathbf{K_T}) = \langle (\tilde{z} - \beta_l \tilde{t})^2 \rangle(\mathbf{K_T}) \,, \tag{3}$$

with $\tilde{x}^\mu(\mathbf{K_T}) = x^\mu - \langle x^\mu \rangle(\mathbf{K_T})$ being the space-time coordinates relative to the momentum dependent *effective source centers*. The average in (1)-(3) is taken over the emission function, i.e. $\langle f \rangle(K) = \int d^4x f(x) S(x,K) / \int d^4x S(x,K)$. In the *osl* system $\beta = (\beta_t, 0, \beta_l)$, where $\beta = \mathbf{K}/E_K$ and $E_K = \sqrt{m^2 + \mathbf{K}^2}$. Below, we cut on midrapidity kaons ($\beta_l \sim 0$), thus the radii are obtained in the *longitudinally comoving frame*. In the absence of $\tilde{x}$-$\tilde{t}$ correlations, i.e. in particular at small K_T, a large duration of emission $\Delta\tau = \sqrt{\langle \tilde{t}^2 \rangle}$ increases $R_{\rm out}$ relative to $R_{\rm side}$ [2–4].

The absolute values of the kaon radii determined by the above expressions (1)-(3) are considerably smaller than the pion radii, especially at low K_T. The pion radii are larger than a factor of *two* at low K_T (≤ 400 MeV) while at higher K_T the values become similar. This is due to the resonance source character of mesons. Microscopic transport calculations show that at SPS energies ($\sqrt{s} = 17.4A$ GeV) about 80% of the pions are emitted from various resonances [21]. This leads to a strong substructure of the freeze-out distributions [21], e.g. strongly non-Gaussian tails. The ratio $R_{\rm out}/R_{\rm side}$ for kaons is shown in Fig. 1. The bag parameter B is varied from 380 MeV/fm^3 to 720 MeV/fm^3, (i.e., the latent heat changes by $\sim 4B$), corresponding to critical temperatures of $T_c \simeq 160$ MeV and $T_c \simeq 200$ MeV, respectively. A change of T_c implies a variation of the longitudinal and transverse flow profiles on the hadronization hypersurface (which is the initial condition for the subsequent hadronic rescattering stage). We find $R_{\rm out}/R_{\rm side}$ to be smaller at the same (small) transverse momentum K_T than the same ratio for pions because of the larger mass of the kaons. At the same low K_T, the velocities of kaons are considerably smaller than those of the pions. Accordingly, the temporal contribution to $R_{\rm out}$ in equation (2) ($\beta_t^2 \langle \tilde{t}^2 \rangle$) is smaller which eventually leads to a smaller ratio $R_{\rm out}/R_{\rm side}$ for kaons at the same low K_T [22]. Thus, for kaons, the ratio increases gradually compared to the rather rapid increase for the pions. While for pions the ratio $R_{\rm out}/R_{\rm side}$ is predicted to reach a value of 1.5 already at $K_T \approx 150\,\mathrm{MeV} \approx m_\pi$

[7] the kaon ratio $R_{\rm out}/R_{\rm side}$ rises to 1.5 only around $K_T \approx 450\,{\rm MeV} \approx m_{\rm K}$. This is again due to the larger mass, that yields smaller flow velocities at smaller K_T than for the pions.

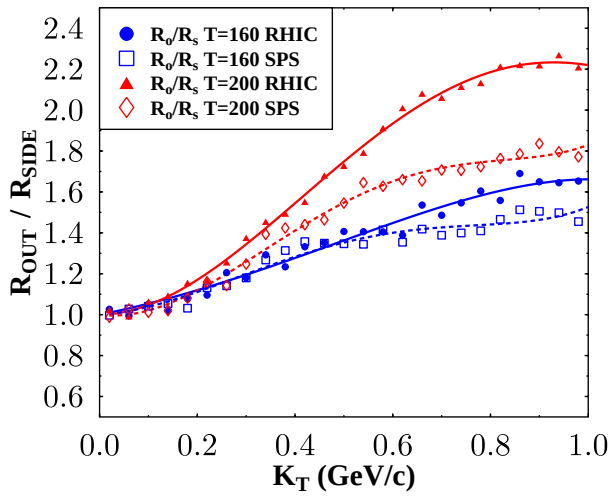

FIG. 1. $R_{\rm out}/R_{\rm side}$ as obtained from eqs. (1) and (2) for kaons at RHIC (full symbols) and at SPS (open symbols), as a function of K_T for critical temperatures $T_c \simeq 160\,{\rm MeV}$ and $T_c \simeq 200\,{\rm MeV}$, respectively. The lines are to guide the eye.

The sensitivity of the value of $R_{\rm out}/R_{\rm side}$ on the critical temperature T_c increases strongly with K_T. Higher T_c speeds up hadronization but on the other hand prolongs the dissipative hadronic phase that dominates the HBT radii. Moreover, in the lower T_c case, direct emission and immediate freeze-out from the phase boundary becomes important at large K_T ($\sim 1\,{\rm GeV/c}$). In other words, the hadronic environment gets less opaque for direct emission. The resonance contribution for the kaons is still quite large, decreasing with K_T from 70 to 50% for $T_c \simeq 160\,{\rm MeV}$. However, most of these kaons are from $K^*(892)$ decays with the K^* having a moderate lifetime of $\tau \approx 4\,{\rm fm/c}$. Elastic scatterings prior to freeze-out contribute on the order of 20%. The direct emission from the phase boundary, i.e., the kaon did not suffer further collisions in the hadron gas after the particle had hadronized, increases strongly (approximately linearly with K_T) for $T_c \simeq 160\,{\rm MeV}$ up to 30% at $K_T = 1\,{\rm GeV/c}$. For the higher $T_c \simeq 200\,{\rm MeV}$ hadronization is earlier, thus the hadronic phase lasts longer and the system gets rather opaque for direct emission. This direct emission component is not present in *pure* ideal hydrodynamical calculations (e.g. [22]) for which all particles, also at high K_T, are in (local) thermodynamical equilibrium. Thus, there is no possibility for direct emission from the phase boundary and escaping the hadronic phase unperturbed.

Finally, we calculate the HBT parameters by performing a χ^2 fit of the three-dimensional correlation function $C_2(q_{\rm out}, q_{\rm side}, q_{\rm long})$ to a Gaussian as

$$C_2(q_{\rm o}, q_{\rm s}, q_{\rm l}) = 1 + \lambda \exp(-q_{\rm o}^2 R_{\rm o}^2 - q_{\rm s}^2 R_{\rm s}^2 - q_{\rm l}^2 R_{\rm l}^2)\,. \quad (4)$$

The correlation functions are calculated from the phase space distributions of kaons at freeze-out using the *correlation after burner* by Pratt [2,20]. It is assumed that the particles are emitted from the large system independently, which allows to factorize the N-boson production amplitude into N one-boson amplitudes $\mathcal{A}(x)$. Then, the emission function is computed as the Wigner tranform $S(x,K) = \int {\rm d}^4y\, e^{iy\cdot K} \mathcal{A}^*(x+y/2)\mathcal{A}(x-y/2)$. The two-boson correlation function is given by

$$C_2(\mathbf{p},\mathbf{q}) - 1 = \frac{\int {\rm d}^4x S(x,\mathbf{K}) \int {\rm d}^4y S(y,\mathbf{K}) \exp\left(2ik\cdot(x-y)\right)}{\int {\rm d}^4x S(x,\mathbf{p}) \int {\rm d}^4x S(y,\mathbf{q})} \simeq \frac{\int {\rm d}^4x S(x,\mathbf{K}) \int {\rm d}^4y S(y,\mathbf{K}) \exp\left(2ik\cdot(x-y)\right)}{|\int {\rm d}^4x S(x,\mathbf{K})|^2}, \quad (5)$$

where $2\mathbf{K} = \mathbf{p}+\mathbf{q}$, $2\mathbf{k} = \mathbf{p}-\mathbf{q}$, and $2k^0 = E_p - E_q$. The second line in (5) holds in the limit where the width of the correlation function is small such that $\mathbf{p} \sim \mathbf{q} \sim \mathbf{K}$.

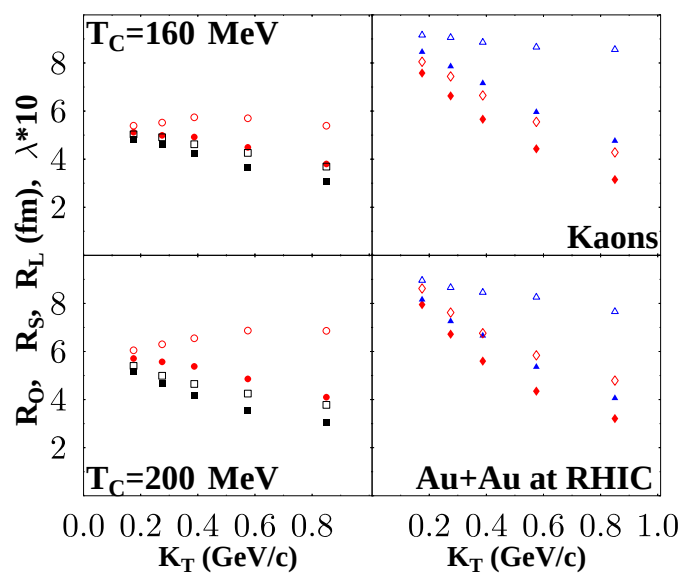

FIG. 2. Kaon HBT-parameters $R_{\rm out}$ (circles), $R_{\rm side}$ (squares), $R_{\rm long}$ (diamonds) and $\lambda \cdot 10$ (triangles) as obtained from a χ^2 fit of C_2 (eq. (5)) to the Gaussian *ansatz* (eq. (4)) for Au+Au collisions at RHIC as calculated with $T_c \simeq 160\,{\rm MeV}$ (top) and $T_c \simeq 200\,{\rm MeV}$ (bottom). Full and open circles correspond to calculations with and without taking momentum resolution effects into account, respectively.

Given a model for a chaotic source described by $S(x,\mathbf{K})$, such as the transport model described above, eq. (5) can be employed to compute the correlation function. While the expressions (1)-(3) based on an Gaussian *ansatz* yield larger values for the pion radii than performing a fit to the correlation functions, for the kaon transverse radii, similar results are obtained with both methods. Only $R_{\rm long}$ is expected to be larger if determined by (3) similar as for the pions because here the non-Gaussian contribution is mainly driven by the longitudinal expan-

sion dynamics that is similar for pions and kaons [23]. Kaons are better candidates for the Gaussian expressions because not only fewer resonance decays are expected to be important for the freeze-out but, moreover, because long-living resonance decays do not play a role as in the pion case. For $T_c \simeq 200\,\mathrm{MeV}$, R_{out} is only approximately 1 fm larger than in the $T_c \simeq 160\,\mathrm{MeV}$ case. This reflects a fact already known from the pions. Higher T_c leads to an earlier hadronization, thus causing a prolonged hadronic phase. When taking finite momentum resolution (*f.m.r.*) into account, the *true* particle momentum p obtains an additional random component. This random component is assumed to be Gaussian with a width δp. The relative momenta of pairs are then calculated from these modified momenta. However, the correlator is calculated with the *true* relative momentum. While R_{out} remains constant or even slightly increases with K_T when calculated without *f.m.r.*, it drops if a *f.m.r.* of $\approx 2\%$ of the center of each K_T bin is considered, a value assumed for the STAR detector [9]. Accordingly, the discrepancies w/o *f.m.r.* increase with K_T. The *f.m.r.* leads to smaller radii. R_{out} is strongly reduced while R_{side} shows a moderate reduction. Thus, the $R_{\mathrm{out}}/R_{\mathrm{side}}$ ratio is considerably reduced through the *f.m.r.*. For example, in the $T_c \simeq 200\,\mathrm{MeV}$ case, it is reduced from 1.8 to 1.35. However, it is always larger than one. The λ parameter is roughly constant as function of K_T for $\delta p/p = 0$ but it decreases rapidly with a *f.m.r.*. This decrease is also seen in recent experimental data at the SPS for Pb+Pb collisions at $\sqrt{s} = 17.4A\,\mathrm{GeV}$ [24]. The *correlation strength is transported to larger q values* by the *f.m.r.* effects.

We have calculated kaon HBT parameters for Au+Au collisions at RHIC energies, assuming a first-order phase transition from a thermalized QGP to a gas of hadrons. No unusually large radii are seen ($R_i \leq 10\,\mathrm{fm}$). A strong direct emission component from the phase boundary is found at high transverse momenta ($K_T \sim 1\,\mathrm{GeV/c}$) where also the sensitivity to the critical temperature, the latent heat and specific entropy of the QGP is enlarged. Finite momentum resolution effects reduce the *true* HBT parameters and the ratio $R_{\mathrm{out}}/R_{\mathrm{side}}$ substantially. Kaon results from RHIC at high K_T will provide an excellent probe of the space-time dynamics close to the phase-boundary and to the properties of this prehadronic state, possibly an equilibrated Quark-Gluon-Plasma.

ACKNOWLEDGMENTS

We are grateful to A. Dumitru, M. Gyulassy, M. Lisa, L. McLerran, S. Pratt, D.H. Rischke, R. Snellings, H. Stöcker, X.N. Wang, and N. Xu for many valuable comments. We thank the UrQMD collaboration for permission to use the UrQMD transport model and S. Pratt for providing the correlation program CRAB. S.S. has been supported by the Humboldt Foundation and DOE Grant No. DE-AC03-76SF00098. S.A.B. acknowledges support from DOE Grant No. DE-FG02-96ER40945.

[1] G. Goldhaber, S. Goldhaber, W. Lee and A. Pais, Phys. Rev. **120**, 300 (1960); E. Shuryak, Phys. Lett. **B44**, 387 (1973); M. Gyulassy, S. K. Kauffmann, L. W. Wilson, Phys. Rev. **C20**, 2267 (1979); A. Makhlin, Y. Sinyukov, Z. Phys. **C39**, 69 (1988); Y. Hama, S. Padula, Phys. Rev. **D 37**, 3237 (1988).

[2] S. Pratt, Phys. Rev. **D33**, 1314 (1986); G. Bertsch, M. Gong, M. Tohyama, Phys. Rev. **C37**, 1896 (1988).

[3] B. R. Schlei, U. Ornik, M. Plümer, R. M. Weiner, Phys. Lett. **B293**, 275 (1992); J. Bolz, U. Ornik, M. Plümer, B. R. Schlei, R. M. Weiner, Phys. Rev. **D47**, 3860 (1993).

[4] D. Rischke, M. Gyulassy, Nucl. Phys. **A608**, 479 (1996).

[5] R. M. Weiner, Phys. Rept. **327**, 249 (2000); T. Csörgő, hep-ph/0001233; G. Baym, Acta Phys. Polon. B **29**, 1839 (1998).

[6] U. Wiedemann, U. Heinz, Phys. Rept. **319**, 145 (1999).

[7] S. Soff *et al.*, Phys. Rev. Lett. **86**, 3981 (2001).

[8] M. Gyulassy, S. Padula, Phys. Rev. C **41**, 21 (1990); Phys. Lett. **B217**, 181 (1989).

[9] STAR Collaboration, C. Adler *et al.*, Phys. Rev. Lett. **87**, 082301 (2001); S. Panitkin, nucl-ex/0106018.

[10] PHENIX Collaboration, S. C. Johnson *et al.*, nucl-ex/0104020; W. A. Zajc *et al.*, nucl-ex/0106001.

[11] C. Greiner, P. Koch, H. Stöcker, Phys. Rev. Lett. **58**, 1825 (1987); Phys. Rev. D **44**, 3517 (1991); C. Spieles *et al.*, Phys. Rev. Lett. **76**, 1776 (1996).

[12] S. Soff *et al.*, J. Phys. G **G23**, 2095 (1997); D. Ardouin *et al.*, Phys. Lett. B **446**, 191 (1999).

[13] H. Von Gersdorff *et al.*, Phys. Rev. **D34**, 2755 (1986).

[14] D. Zschiesche *et al.*, nucl-th/0107037.

[15] T. Csörgő, L.P. Csernai, Phys. Lett. B **333**, 494 (1994); H. Heiselberg, A. D. Jackson, nucl-th/9809013; A. Dumitru, R. Pisarski, Phys. Lett. **B504**, 282 (2001); O. Scavenius *et al.*, Phys. Rev. D **63**, 116003 (2001); hep-ph/0103219.

[16] A. Dumitru and D. Rischke, Phys. Rev. **C59**, 354 (1999).

[17] S. A. Bass, A. Dumitru, Phys. Rev. **C61**, 064909 (2000).

[18] S. A. Bass *et al.*, Prog. Part. Nucl. Phys. **41**, 255 (1998); M. Bleicher *et al.*, J. Phys. **G25**, 1859 (1999).

[19] Review of Particle Physics, Eur. Phys. J. **C3**, 1 (1998).

[20] S. Pratt, T. Csörgő, J. Zimanyi, Phys. Rev. C **42**, 2646 (1990); S. Pratt, Phys. Rev. Lett. **53**, 1219 (1984); Phys. Rev. **C49**, 2722 (1994); W. A. Zajc, Phys. Rev. D **35**, 3396 (1987); S. Pratt *et al.*, Nucl. Phys. **A566**, 103c (1994).

[21] S. Soff *et al.*, CRIS'98, Acicastello, Italy, 1998; proceedings *Measuring the size of things in the universe: HBT interferometry and heavy ion physics*; edited by S. Costa *et al.*, World Scientific, (1999), 221-233.

[22] S. Bernard *et al.*, Nucl. Phys. A **625**, 473 (1997).

[23] D. Hardtke, S. Voloshin, Phys. Rev. C **61**, 024905 (2000).

[24] NA44 Collaboration, I. G. Bearden *et al.*, Phys. Rev. Lett. **87**, 112301 (2001).